J. Gallaway-Booth, J. Cohen, V. McKay-Crites, C. Martz, S. Van Middlekoop, A. Tillie,

Supervisors: Ioannis Haranas and Ilias Kotsireas Dept. of Physics and Computer Science, Wilfrid Laurier University Science Building, Waterloo, ON, N2L 3C5.

e-mail:iharanas@wlu.ca, mcka8980@mylaurier.ca, Mart4200@mylaurier.ca. Gall5030@mylaurier.ca,

kotsireas@wlu.ca, vanx0250@mylaurier.ca, till9960@mylaurier.ca. Cohe4750@mylaurier.ca

Abstract

Among nature's cosmic catastrophes can be the ones caused by a falling meteorites/asteroids of considerable sizes. In this presentation we examine two different of meteorite sizes falling at the ocean. Thus, we study the effect that the Earth's corrected gravity for geocentric latitude, J₂ harmonic (oblatness) and rotation has upon impact in the depth of a created crater, as well a in its radius. We have found that that the total correction effect of geocentric latitude, oblateness, and rotation results to a 0.30% increase in the depth of the crater if the impact occurs at the equator when compared to a fall at the poles. Similarly the radius increases by 0.12% if the impact occurs at the equator. We conclude that meteoric/asteroid impacts at the equator will results to more catastrophic results and higher tsunami heights when compares to those of polar impacts.

Introduction

Progress in celestial mechanics and solar system dynamics in the twentieth and twenty-first centuries resulted in the extensive study of various solar system meteorite bodies, so that their orbits and possible scenario of meteorite collision course could be determined. Furthermore accumulation of solar system knowledge coming from various missions played an important role in determining the possibility of a possible meteoric collision with the Earth.

We now know that meteoric sizes vary from tens of meter to kilometers. A considerable number of these bodies approaches the Earth to very close distances, some of which are comparable to the Earth -Moon distance. Collision of large bodies with the Earth is truly a rare event, where collision with smaller bodies as well as medium sized bodies, have happened quite often in the past. Earth has often collided with meteoritic bodies something that expected to double every 5.8 years. So far we have knowledge of approximately two hundred craters which due to data inconsistency can probably double Kozelknov et al. (2015).

Asteroid and comet impacts have also played a major role in the biological and geological history of the Earth. In particular we say that two thirds of the space objects that fall on the Earth end up impacting the water, thus the possibility of a tsunami creation that can be propagated in great distances, is a very probable event. These are the tsunamis that are created due to the collapse of pelagic impact cavities (Hills at al. 1994), and (Nemtchinov et al. 1997). Finally, we say that our planet exhibits evidence of asteroid impacts and impact tsunamis as well. As an example we mention that Gersonde et al. (1997) have documented the collision of a 1km or probably larger in diameter in the asteroid in the south ocean during the late Pliocene (2.15 Ma). In this paper we examine the effect that corrected gravitational acceleration has upon impact in the meteorite crater depth as well as upon it's the crater radius, for two meteorites of 50 and 100 m respectively.





The effect of corrected gravitational acceleration in the depth and diameter in tsunamis of meteoric origin

Asteroid impact tsunami theory basics and initial cavity shape specifics modeling method

The tsunami energy increases when water mass is deposited on the lids of the created cavity, which at the same time increases the energy of the cavity. The additional energy is composed of shorter length waves than the cavity's diameter, and it results in slow travelling that does not increase the tsunami's peak amplitude. Following (Ward and Asphaug, 2000), and for initial transient cavities i.e. cavities where all the water is deposited into the lip, would imply that and therefore there is no net water loss, and therefore we can write that the depth of the cavity is

furthermore, assuming a general relationship between cavity and radius to be (Ward of depth D and radius R, that eventually starts the tsunami activity, and Asphaug, 2000). The radius of the cavity is given by the equation:

$$R_{c} = R_{i} \left(\frac{2\varepsilon V_{i}^{2}}{gR_{i}} \right)^{\delta} \left(\frac{\rho_{i}}{\rho_{w}} \right)^{\frac{1}{3}} \left[\left(\frac{\rho_{w}}{\rho_{i}} \right)^{\frac{1}{3} - \delta} \left(\frac{1}{gR_{i}^{n-1}} \right)^{2\delta} \right]$$

The gravitational acceleration on the surface of the Earth and at orbital point

In our effort to study the effect of gravity on the depth and radius of the cavity if any, let us consider a corrected acceleration of gravity g. This would imply that we will take into account the dependence of gravitational acceleration a) on geocentric latitude and b) on the Earth's oblateness that is expresses via the J2 harmonic coefficient, and finally the rotation of the Earth Following Haranas, et al., (2012, 2015) we write the acceleration of gravity as the sum of

$$g(\phi) = \frac{GM_E}{R_{eq}^2 \left(1 - f' \sin^2 \phi \right)^2} - \frac{3GM_E J_2 \left(3 \sin^2 \phi - 1 \right)}{2R_{eq}^2 \left(1 - f' \sin^2 \phi \right)} - R_{eq} \omega_E^2 \left(1 - f' \sin^2 \phi \right) \cos^2 \phi$$

where is the radial distance from the center of the Earth to an external surface point, ME is the mass of the Earth, RE is the radius of the Earth, J2 is the zonal harmonic coefficient that describes the oblateness of the Earth, the angular velocity of the Earth, and de the geocentric latitude of the meteorite falling site. Zonal harmonics are simply bands of latitude, whose boundaries are the roots of a Legendre polynomial. Spherical harmonics in general are very important concept in solar system research and in particular in the modelling of planetary gravity fields. For example in Hadjifotinou (2000) the author uses a gravitational potential that includes a J2 as well as a J4 harmonics in predicting numerically the motion of Saturn's satellites. Similarly, in Jorio (2011) the author derives the precession of the ascending node of a satellite due to Lense-Thirring effect as a function of the J2 harmonic. This particular gravitational harmonic coefficient is a result of the Earth's shape and is about 1000 times larger than the next harmonic coefficient J3 and its value is equal to $J_2 = 0.0010826269$ (Vallado and McCain, 2000).

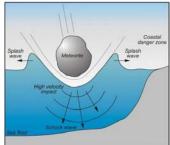


Figure 1 Meteorite falling in the ocean and creating a crater

To proceed with our numerical calculation let us assume the following values for the parameters entering our calculations, $M_F =$ 5.9742×10^{24} kg is the mass of the Earth, and $R_E = 6378.1363$ km is the radius of the Earth, $J_2 = 0.0010826269$ (Vallado and Mac Cain, 2007), f = 0.003353813178 is the flattening coefficient of the Earth. $\omega_E = 7.292115 \times 10^{-5}$ rad/s is the rotational velocity of the Earth (ibid, 2007). Furthermore, we assume meteorites with radii $R_i = 50$, 100, 500 m respectively, and q = 0.10, 0.083, 0.054 (Ward and Asphaug, 2000) of density $\rho_i = 3000 \text{ kg/m}^3$, and a Schmidt-Holsapple parameter $\beta = 0.22$ (Ward and Asphaug, 2000), which has a physical connection to the aspect ratio of a crater and if the impact energy conversion factor holds rather constant at approximately ≈ 15%, finally from laboratory experiments in water $\alpha = 1.27$ (Ward and Asphaug, 2000).

First we calculate the depth of cavity upon impact with constant acceleration of gravity $g = 9.81 \text{ m/s}^2$, for two meteorites with radius R_i = 50 and 100 m respectively and with corresponding q's = 0.10 and 0.083 (Ward and Asphaug, 2000), density $\rho_i = 3000 \text{ kg/m}^3$, $V_i = 20$ km/s, $\varepsilon = 16\%$. We have assumed that the meteorites fall in the ocean with density $\rho_{w} = 1027 \text{ kg/m}^3$ and therefore we obtain that the cavity's corresponding depths are D = 1292.32 m and 2128.86 m respectively. These numbers are in very close agreement with the results given in (Ward and Asphaug, 2000). Similarly, taking into account the corrected gravitational acceleration i.e. J2 and rotation of the Earth we find the results tabulated in table 1 below using the modified gravity corrected formula given above the tablre:



Table 1 Corrected gravity cavity depth effect for a 50 m and 100 diameter meteorite at various geocentric latitudes

Geocentric	Uncorrected	Uncorrected	Corrected Gravity	Corrected Gravity
Latitude	Gravity Cavity	Gravity Cavity	Cavity Depth	Cavity Depth
φ [deg]	Depth	Depth Calculation	Calculation	Calculation
	Calculation	D[m]	D[m]	
	D[m]			D [m]
	Meteorite	Meteorite	Meteorite	Meteorite
	Diameter	Diameter	Diameter	Diameter
	50 m	100 m	50 m	100 m
0			1294.48	2132.42
30	1292.32	212886	1293.62	2131.00
45			1292.76	2129.59
60			1291.91	2128.19
90			1291.07	2126.79



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Table 2 Corrected gravity cavity radius effect for a 50 m, and 100 diameter meteorite at various geocentric latitudes

Geocentric	Uncorrected	Uncorrected	Corrected Gravity	Corrected Gravity
Latitude	Gravity Cavity	Gravity Cavity	Cavity Radius	Cavity Radius
φ [deg]	Radius	Radius Calculation	Calculation	Calculation
	Calculation R[m]	R [m]	R [m]	R [m]
	Meteorite	Meteorite	Meteorite	Meteorite
	Diameter	Diameter	Diameter	Diameter
	50 m	100 m	50 m	100 m
0			1693.54	2910.99
30	1692.29	2908.84	1693.04	2910.13
45			1692.55	2909.28
60	1		1692.06	2908.44
90	7		1691.57	2907.60

Conclusions

Correcting the Earth's gravitational acceleration for the latitude dependence, oblateness and rotation we have found that upon impact a falling into the ocean meteorite results to a crater depth and radius that is higher at the equator and smaller at the poles . The % difference for meteorite considered between the depth at the equator and that at the poles is approximately 0.30% where between the radius for the same geocentric locations is about 0.12%. This would imply, that a meteorite/asteroid if fell at the equator given its size and velocity would create a grater depth and diameter crater which potentially will result in a higher maximum tsunami height.

References

[Dingemans, W. M., 1997, Water Wave Propagation Over Uneven Bottoms: Linear wave propagation, World Scientific Publishing

Gersonde, R. et al. (1997) Nature, 390, 357-363.

Haranas I., Gkigkitzis, I., Zouganelis D., G., g Dependent particle concentration due to sedimentation, Astrophys. and Space Sci. DOI 10. 1007/s10509-012-1151-1, 2012.

Haranas I., Gkigkitzis, I., Kotsireas I., Haranas M. K., Rekkas I., The effect of gravitational acceleration in the streaming potential on the surface of planetary body and in orbit around it, Advances in Space Research, 56 (2015), 1714-1725.

Hills J. G., Nemtchinov, I. V., Popov, S. P., and Teretev, A. V., 1994 Tsunami generated by small asteroid impacts. In Hazards due to comets and asteroids, ed T. Gehrels University of Arizona Press,

Hadjifotinou, K. G., Numerical integration of satellite orbits around an oblate planet, Astronomy and Astrophysics, v.354, p.328-333,

Kozelkov A. S., Kurkin A. A., E. N., Pelinovskii and Kurulin V. V., (2015) Modeling the cosmnogenic tsunami within the framework of Navier-Stokes equations with sources of different types // Fluid Dynamics 2015 v 50 303-313

Nemtchinov I.V., Jacobs C., Tagliaferri E., 1997. Analysis of satellite observations of large meteoroid impacts. Annals of New York Academy of Sciences 822, 303-317. Menahem, A. B., Singh S. J., 1981 Seismic Waves and Sources, Springer-Verlag, 2nd

Ward S. N., and Asphaug 2000, E., Asteroid impact tsunami: a probabilistic hazard assessment, Icarus, v. 145, 64-78.

